

↑ Bracket
 → division
 → Addition
 ↓ subtraction
 ↓ multiplication
 ↓ order
 ① BODMAS

$$(i) 4(10+15 \div 5 \times 4-2+2)$$

$$4(10+3 \times 4-2+2)$$

$$4(10+12-2+2)$$

$$4(22-2+2)$$

$$4(24-2)$$

$$4(22)$$

$$= 88$$

$$4(22-2+2)$$

$$= 4(24-2)$$

$$= 4(22)$$

$$= 88$$

$$\begin{array}{r} 14 \\ \times 3 \\ \hline 42 \end{array}$$

$$(ii) 14+26-27 \div 3 \times 2$$

$$14+26-9 \times 2$$

$$14+26-18$$

$$= 40-18$$

$$= 22$$

$$(iii) 3+24 \times (15 \div 5)$$

$$3+16 \times 3$$

$$3+48$$

$$51$$

$$\text{---} \rightarrow \text{①}$$

$$\text{---} \rightarrow \text{②}$$

$$\boxed{\quad} \rightarrow \text{③}$$

round
curly
square

Exponents / power

A mathematical notation that represent number of time a base should be multiplied e.g

$$x \begin{matrix} \leftarrow \text{power} \\ \leftarrow \text{base} \end{matrix} = x \cdot x \cdot x \cdot x \cdot x$$

$$3^2 = 3 \times 3 = 9$$

$$2^4 = 2 \times 2 \times 2 \times 2 = 16$$

$$2^4 \times 3^2 = 16 \times 9 = 144$$

Multiplication :-

same variables / bases

$$x^3 \times x^2 = x^5$$

when bases are same powers are added

$$y^1 \times y^5 = y^6$$

when bases are different

$$x^2 \times y^3 = x^2 y^3$$

② power raised to the power

$$(2^2)^3$$

$$= 2^6$$

$$= 64$$

$$(a^b)^c$$

$$= a^{bc}$$

5/16/9
14/9

Date: _____

Fraction form of power

$$\frac{x^2}{y^3} \begin{array}{l} \longrightarrow \text{numerator} \\ \longrightarrow \text{denominator} \end{array} = \frac{y^{-3}}{x^2}$$

$$= x^2 y^{-3}$$

$$\frac{x}{y} = \frac{y^{-1}}{x^{-1}}$$

$$\frac{x^{-2}}{y^3} = \frac{y^3}{x^2}$$

Zero Exponent:-

Any number/base raised power zero, the result will be 1

$$2^0 = 1$$

$$100^0 = 1$$

$$(543268)^0 = 1$$

$$(x^2 y^3 z^6)^0 = 1$$

$$\sqrt[n]{\quad} = \frac{1}{n}$$

$$\sqrt[3]{\quad} = \frac{1}{3}$$

$$\sqrt[4]{\quad} = \frac{1}{4}$$

Square root

$$\begin{aligned} \sqrt{\quad} &= \frac{1}{2} \\ \sqrt{4} &= (4)^{\frac{1}{2}} \\ &= (2^2)^{\frac{1}{2}} \\ &= 2 \end{aligned}$$

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Additive inverse "0"

Changing the sign of the number and adding it to the original number

(i) $5, -5$

$$5 - 5 = 0$$

$$\begin{array}{l} +x - = - \\ -x + = - \\ -x - = + \\ +x + = + \end{array}$$

(ii) $x^2, -x^2$

$$x^2 - x^2 = 0$$

Multiplicative inverse: (1)

A number when multiply with the original number yields (1)

$$\cancel{5} \times \frac{1}{\cancel{5}} = 1$$

$$\cancel{x^2} \times \frac{1}{\cancel{x^2}} = 1$$

Number system:-

(i) Natural number:-

Counting number starting from 1 upto infinity all called natural numbers it is denoted by "N"

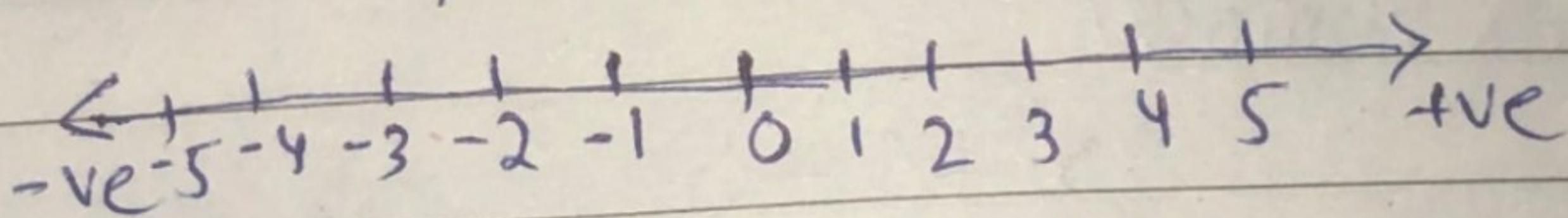
$$N = \{1, 2, 3, \dots, \infty\}$$

② Whole numbers:-

counting number starting from 0 upto infinity all called whole number it is denoted by W
 $W = \{0, 1, 2, 3, \dots\}$

③ integers:-

Natural number and their Additive inverse. It has no Fraction or decimal form it is denoted by "Z"



natural number and its additive inverse called integers

④ Rational numbers:-

Number that can be written in the form of $\frac{p}{q}$ are called rational numbers. It

is denoted by "Q"

$\frac{7}{9}, \frac{3}{2}, \frac{8}{5}$

$\frac{3.2}{4.628531\dots}$

Terminating Form = Jahan number end ho after 4 or 5 digit.

non-terminating / recurring = $1.\overline{3333}\dots$
 $= 1.\overline{242424}\dots$

- if specific number

$\frac{22}{7} = \frac{22}{7} = \frac{p}{q} \rightarrow$ rational number repeat

$\frac{22}{7} = 3.142857 \rightarrow$ non-terminating and non recurring called irrational number. we can't write in $\frac{p}{q}$ form

non terminating and recurring number called rational number.

⑤ Real number:

it is the combination of derived, rational, irrational, natural, whole number
 $3, 0, \frac{1}{2}, -\frac{1}{4}, 3.2 \dots$

⑥ Complex number

$$x^2 + 1 = 0$$

$$x^2 = -1$$

$$\sqrt{x^2} = \sqrt{-1}$$

$$x = \sqrt{-1} = i \rightarrow \text{iota}$$

$$i = \sqrt{-1}$$

$$i^2 = -1$$

it is the combination of real and imaginary number called complex number. it denoted by Z

$$Z = a + bi \quad \begin{array}{l} \nearrow R \quad \nearrow I \\ i \quad 2 + 3i \end{array}$$

real
imaginary

(i) $2 + 3i + 2 + 4i = 4 + 7i$ (ii) $2 + 3i + 4 + 3i = 6 + 6i$

(7) Even number:

Number that are divisible by 2 are called even numbers

$$E = \{2, 4, 6, 8, 10, 12, \dots\}$$

• zero is also even number
i.e. $\frac{0}{2} = 0$

(8) Odd number:

Number that are not divisible by 2 are called odd numbers

$$O = \{1, 3, 5, 7, 9, 11, \dots\}$$

(9) Prime number:

Number that are divisible by 1 and itself are called prime numbers

$$2, 3, 5, 7, 11$$

Composite numbers are those which are not prime numbers and 1 is not a prime number, zero is neither prime nor composite.

4 → 1, 2, 4
↓
its not prime
its composite
number

Arithmetic of decimal numbers:-

(i) Addition of decimal numbers

$$12.5 + 6.23 = 18.73$$

$$14.7 + 3.685 = 18.385$$

$$13.64 + 5.431 + 3.82 = 22.891$$

$$\begin{array}{r} 1 \\ 14.7 \\ + 3.685 \\ \hline 18.385 \end{array}$$

~~13.64~~

$$\begin{array}{r} 12.5 \\ + 6.23 \\ \hline 18.73 \\ 13.64 \\ + 5.431 \\ + 3.82 \\ \hline 22.891 \end{array}$$

② Subtraction of decimal number

(i) $8.5 - 6.23 = 2.27$

$$\begin{array}{r} 8.50 \\ - 6.23 \\ \hline 2.27 \end{array}$$

(ii) $7.5 - 4.368$

$$\begin{array}{r} 7.500 \\ - 4.368 \\ \hline 3.132 \end{array}$$

(iii) $5.3 - 2.8$

$$\begin{array}{r} 5.3 \\ - 2.8 \\ \hline 2.5 \end{array}$$

(i) Subtracting whole number from decimal

$$8.3 - 5$$

$$\begin{array}{r} 8.3 \\ - 5.0 \\ \hline 3.3 \end{array}$$

(ii) Subtracting decimal from whole number

(i) $9 - 4.2$

$$\begin{array}{r} 9.0 \\ - 4.2 \\ \hline 4.8 \end{array}$$

(ii) $9.6 - 4.17$

$$\begin{array}{r} 9.60 \\ - 4.17 \\ \hline 5.43 \end{array}$$

3/6/23
2/2/1
1/1/1
~~6/2/4~~

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(ii) Decimal multiplication

(i)

$$\begin{array}{r} 6.4 \times 3.1 \\ \underline{6.4} \\ 19.2 \\ \hline 19.84 \end{array}$$

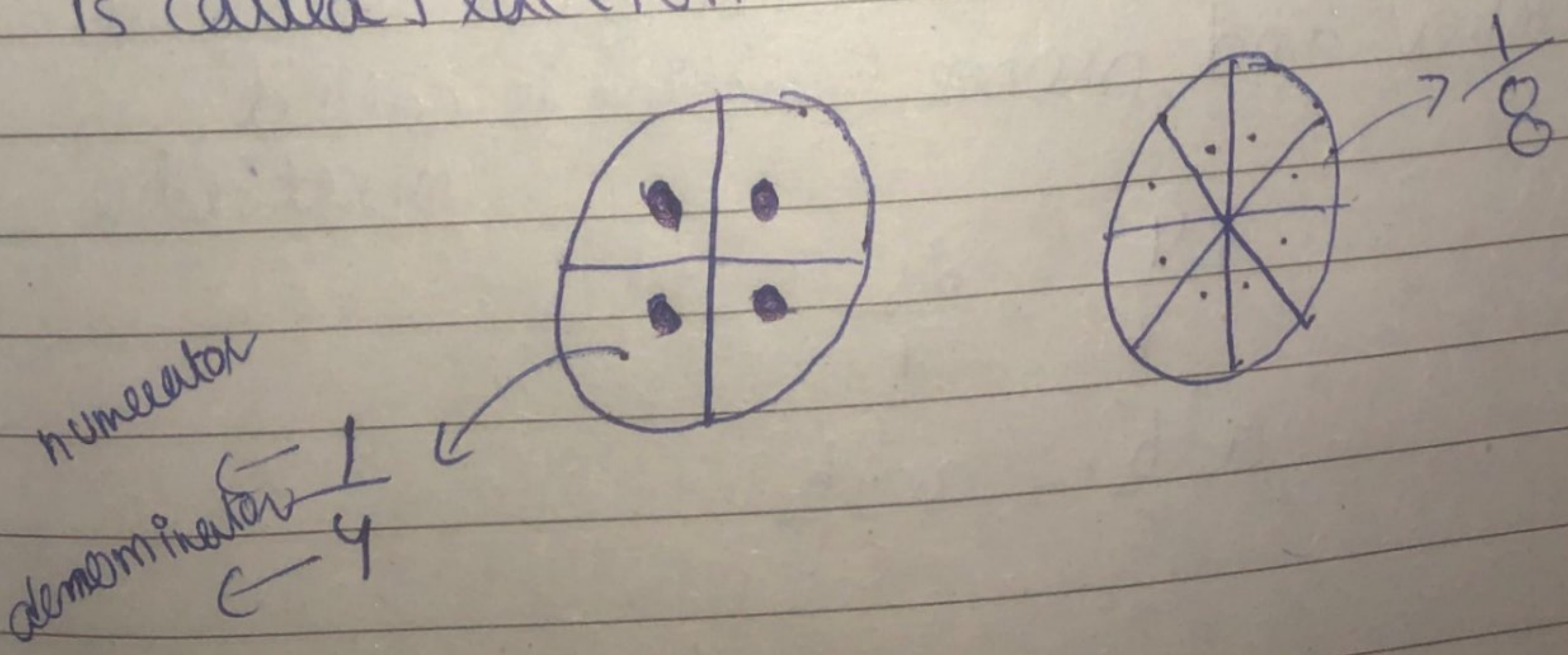
(ii)

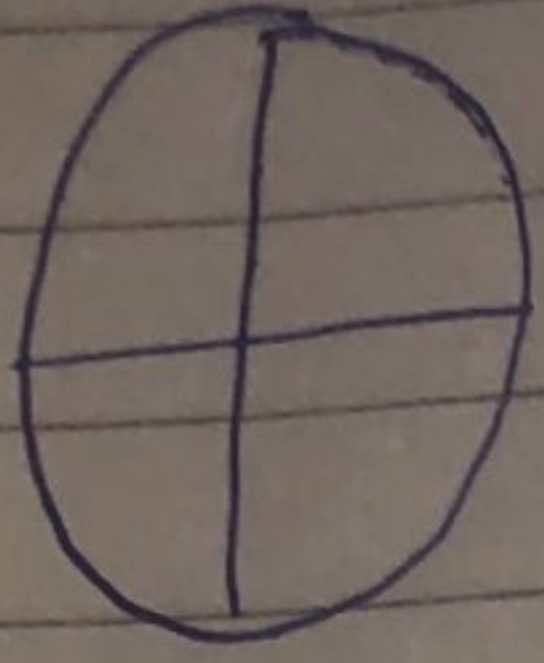
$$\begin{array}{r} 11.3 \times 2.5 \\ \underline{11.3} \\ 226 \\ \hline 28.25 \end{array}$$

$$\begin{array}{r} 76 \\ 0.9 \\ \underline{8.7} \\ 63 \\ 72 \\ \hline 7.83 \end{array}$$

Fraction:-

A small or tiny portion of something is called fraction.





$$\frac{2}{3} \rightarrow \text{i.e. } \frac{2}{3} \text{ of majority}$$

$$\frac{3}{4}$$

~~Types~~ Types of fraction

① ~~proper~~ ~~fraction~~ ~~fraction~~:
~~proper~~ ~~fraction~~ ~~fraction~~

A fraction in which numerator is less than the denominator

$$\frac{4}{5}, \frac{3}{7}, \frac{x^2}{x^3}$$

② improper fraction:

A fraction in which numerator is either equal or greater than the denominator.

$$\frac{8}{5}, \frac{3}{2}$$

③ mixed fraction:-

A combination of natural number and proper fraction is called mixed fraction

$$3\frac{4}{7} = \frac{25}{7}$$

$$a\frac{b}{c} = \frac{ac+b}{c}$$

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$$\begin{array}{r} 1 \\ 500 \\ \hline 103 \end{array}$$

Arithmetic of fraction: -

① Addition of fraction

$$\frac{1}{16} + \frac{3}{16} + \frac{5}{16} = \frac{1+3+5}{16} = \frac{9}{16}$$

$$\frac{1}{2} + \frac{3}{5} + \frac{7}{3} = \frac{15+18+70}{30} = \frac{103}{30}$$

② Subtraction of fraction

$$\frac{2}{3} - \frac{1}{3} = \frac{2-1}{3} = \frac{1}{3}$$

$$\frac{1}{2} - \frac{3}{7} = \frac{7-6}{14} = \frac{1}{14}$$

③ Multiplication of fraction

$$\frac{5}{3} \times \frac{2}{4} = \frac{10}{12} = \frac{5}{6}$$

④ Division of fraction

$$\begin{aligned} \frac{1}{6} \div \frac{1}{3} \\ = \frac{1}{6} \times \frac{3}{1} \\ = \frac{3}{6} \\ = \frac{1}{2} \end{aligned}$$

$$\begin{array}{r}
 420 \\
 \times 15 \\
 \hline
 2100 \\
 2100 \\
 \hline
 6300
 \end{array}$$

LCM & HCF

↓
least
Common
multiple

↓ highest
common
factor

$$\begin{array}{r}
 2 \overline{) 28} \\
 \underline{2 14} \\
 7 7 \\
 \underline{7 7} \\
 1
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 70} \\
 \underline{5 35} \\
 7 7 \\
 \underline{7 7} \\
 1
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 84} \\
 \underline{2 42} \\
 3 21 \\
 \underline{3 21} \\
 7 7 \\
 \underline{7 7} \\
 1
 \end{array}$$

$$\begin{aligned}
 28 &= 2 \times 2 \times 7 \\
 70 &= 2 \times 5 \times 7 \\
 &= 2 \times 2 \times 3 \times 7
 \end{aligned}$$

$$\begin{aligned}
 \text{HCF} &= 2 \times 7 = 14 \\
 \text{LCM} &= 2 \times 2 \times 7 \times 5 \times 3 \\
 &= 420
 \end{aligned}$$

Find the LCF & HCF 24 & 36

$$\begin{array}{r}
 2 \overline{) 24} \\
 \underline{2 12} \\
 2 6 \\
 \underline{2 6} \\
 3 3 \\
 \underline{3 3} \\
 1
 \end{array}$$

$$\begin{array}{r}
 2 \overline{) 36} \\
 \underline{2 18} \\
 3 9 \\
 \underline{3 9} \\
 3 3 \\
 \underline{3 3} \\
 1
 \end{array}$$

$$\begin{aligned}
 24 &= 2 \times 2 \times 2 \times 3 \\
 36 &= 2 \times 2 \times 3 \times 3
 \end{aligned}$$

$$\begin{aligned}
 \text{HCF} &= 2 \times 2 \times 3 = 12 \\
 \text{LCM} &= 2 \times 2 \times 3 \times 2 \times 3 \\
 &= 72
 \end{aligned}$$

$$\begin{array}{r}
 1 \\
 24 \\
 + 36 \\
 \hline
 72
 \end{array}$$

Find the greatest number that divides 204 & 64 without a remainder

$$\begin{array}{r|l}
 2 & 204 \\
 \hline
 2 & 102 \\
 \hline
 3 & 521 \\
 \hline
 17 & 17 \\
 \hline
 & 1
 \end{array}$$

$$\begin{array}{r|l}
 2 & 64 \\
 \hline
 2 & 32 \\
 \hline
 2 & 16 \\
 \hline
 2 & 8 \\
 \hline
 2 & 4 \\
 \hline
 2 & 2 \\
 \hline
 & 1
 \end{array}$$

$$204 = 2 \times 2 \times 3 \times 17$$

$$64 = 2 \times 2 \times 2 \times 2 \times 2 \times 2$$

$$\text{HCF} = 2 \times 2 = 4$$

$$\text{LCF} = 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 3 \times 17 =$$

Division of decimal number

$$8.5 \div 3.4 = 2.5$$

$$\begin{array}{r}
 2.5 \\
 34 \overline{) 85} \\
 \underline{68} \\
 170 \\
 \underline{170} \\
 \text{xx}
 \end{array}$$

$$\begin{array}{r}
 34 \\
 \times 2 \\
 \hline
 68 \\
 \\
 2 \\
 34 \\
 \times 5 \\
 \hline
 170
 \end{array}$$

$$10.8 \div 1.5$$

$$\begin{array}{r}
 7.2 \\
 15 \overline{) 108} \\
 \underline{105} \\
 \text{x} 30 \\
 30 \\
 \hline
 \text{xx}
 \end{array}$$