

CSS-2023 physics Paper I

(Part-II)

Q NO. (Part-a)

What is Gradient of a scalar function?

Give its physical significance and show

the Gradient $\text{Grad } \phi = \nabla \phi$

When we measure the change

in a scalar field with a

particular direction. In other

words the rate of change

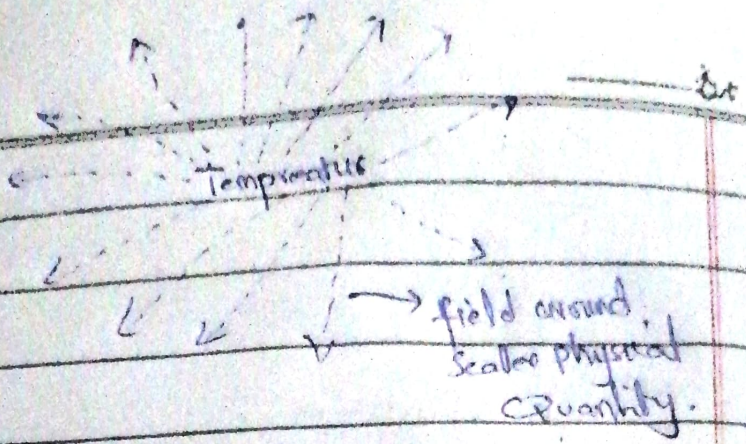
of the scalar field ~~at~~

is known as "gradient".

For example: Temperature is a scalar quantity. But when we measure the change in temperature in a particular direction. This becomes gradient.

∇

Mathematical expression of the gradient of temperature:



measuring it the field of temperature with different angle

Give the derivation as well

$$\nabla T = \frac{\partial T}{\partial x} + \frac{\partial T}{\partial y} + \frac{\partial T}{\partial z}$$

Physical Significance of the Gradient:

it is a primary concept in physics. because through gradient we can measure change and the rate of change in a scalar field.

- (a) The field of temperature...
- (b) The electric potential $\Delta V = E$
- (c) The Heat flow $\Delta T = H$

these are significant phenomena that can be deal with the help of gradient

attempt in detail by giving subheading

[Q2, Part - b]

Q) Acceleration and its cartesian components:

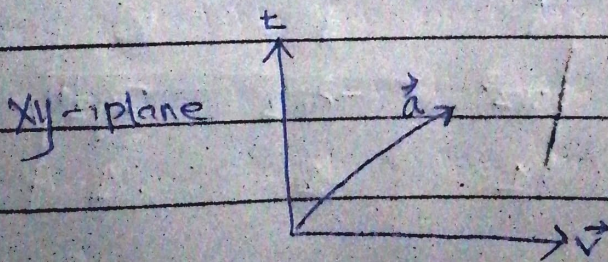
The rate of change in velocity is known as acceleration.

Math. mathematical Representation:

$$\vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

Vector quantity because the division of vector with a scalar is again a vector quantity.

Cartesian components of Acceleration



As here in xy-plane the Cartesian component the acceleration

$$\text{if } \vec{a} = a_x \hat{i} + a_y \hat{j}$$

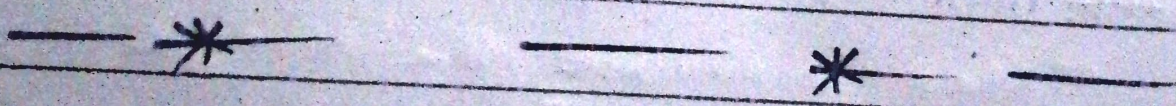
Detailed derivation?

while $a_x = a \cos \omega t$

$$a_y = a \sin \omega t$$

while in the cartesian components of acceleration are:

$$\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$$



Q No 2 (Part - a c)

$$\vec{A} = xz^3 \hat{i} - 2x^2z \hat{j} + 2y^2 \hat{k}$$

So find curl at the point (1, -1, 1)

Ans: $\text{curl } \vec{A} = \nabla \times \vec{A} =$

Q No 2 (Part - c)

$$\vec{A} = xz^3\hat{i} - 2x^2z\hat{j} + 2yz^4\hat{k}$$

then find curl of A at the point
(1, -1, 1)

$$\nabla \times A = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ xz^3 & -2xz & 2yz^4 \end{vmatrix}$$

Now operating the formula.

$$\hat{i} \left[\frac{\partial}{\partial y} (2yz^4) - \frac{\partial}{\partial z} (-2xz) \right]$$

$$\hat{j} \left[\frac{\partial}{\partial x} (2yz^4) + \frac{\partial}{\partial z} (xz^3) \right]$$

$$\hat{k} \left[\frac{\partial}{\partial x} (-2xz) - \frac{\partial}{\partial y} (xz^3) \right]$$

$$\hat{i} [2z^4 + 2x] - \hat{j} [2xz^3] + \hat{k} [-2z]$$

if by calculating:

$$[2z^4 + 2x]\hat{i} - 2xz^3\hat{j} - 2z\hat{k}$$

Now to put the value (1, -1, 1)

$$4\hat{i} + 3\hat{j} - 2\hat{k} = \nabla \times A \text{ at a point}$$

Write the final answer in the form
of statement

Attempt and upload a single qs at a time for evaluation

QNOB4:

Part a):

what was physics like before relativity and how did Einstein come up with his theory? mathematically explain how mass and energy is interchangeable?

Ans: This statement can be answered in three different segment. The first will answered the classical physics era / Newtonian era. while the second one, physics transition era of transition bet from classical to modern physics. and the third one is the mass-energy conversion assumption of theory of relativity.

(i) physics before the theory of Relativity:

Before the era of theory Relativity. There were mainly three area of physics that was:

- (a) Classical Mechanics
- (b) Optics
- (c) Classical thermodynamic

Scientist used to consider these three fields as parameter for the rest of natural phenomenon. On the basis of these assumption. The whole physics ~~was~~ ~~is~~ central ideas:

- (i) Time is an absolute quantity
- (ii) Length is not changed.
- (iii) The presence of ether that propagate light waves.

(ii) How did Einstein come up his theory?

Einstein

In that time, physics faced several natural phenomena, which it unable to response. For example, the newtonian physics, studying it with difference reference frame, and maxwell's equation and the most important one was the Michelson - interferometer experiment.

Then Einstein came up with the theory of relativity to response these question. So that it laid

down a ~~new era~~ base of a
new era in physics.

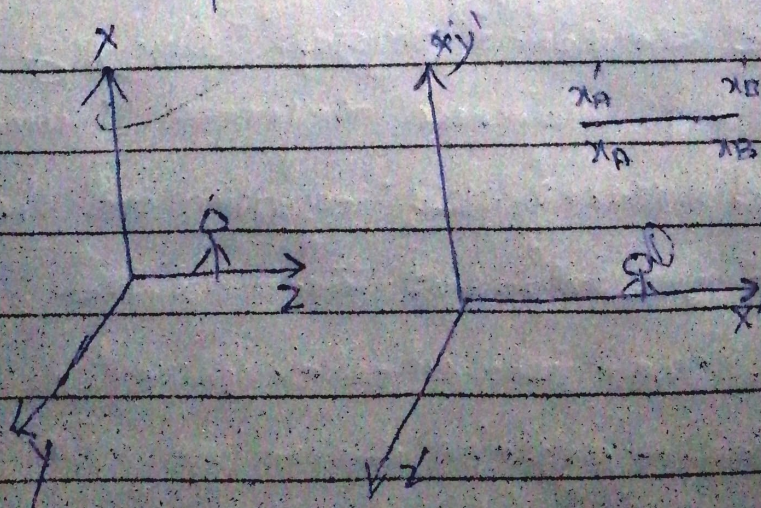
Q no 4 part-b:

pe "Einstein Assumption of Relative length"

Einstein rejected the Newton assumption of length. According to him, length is absolute physical quantity.

~~But Einstein~~ According to the Einstein theory of Relativity, ~~motion in~~ ~~length~~ observing from different reference frame is vary according to observer. In a nutshell, motion impacts the length of a body while observing from different reference

frame: for example,



According to observer 1, the length of the rod is $\Delta L_0 = x'_B - x'_A$ while the observer "2" it is different. let to elaborate:

$$x'_A = \gamma(x_A - v_A t)$$

$$x'_B = \gamma(x_B - v_B t)$$

Putting in the above equation

$$\Delta L_0 = \gamma(x_B - v_B t) - \gamma(x_A - v_A t)$$

$$\Delta L_0 = \gamma x_B - \gamma v_B t - \gamma x_A + \gamma v_A t \rightarrow 0$$

$$\Delta L_0 = \gamma x_B - \gamma x_A - \gamma(v_B t - v_A t)$$

$$\Delta L_0 = \gamma(x_B - x_A)$$

$$\Delta L_0 = \Delta L \gamma \quad \therefore \gamma = \sqrt{1 - \frac{v^2}{c^2}}$$

* ————— *

Q) no 4 (Part-c)

Calculate the mass equivalent of Energy from an antenna radiating 20 kW for 24 hours.

Given Data in the statement:

- Energy Radiated by antenna 20 kW
- ⇒ During 24 hours

what is the required data according to the statement:

To determine how much energy is being radiated during 24 hours and the emission

The Equivalence of mass of that energy which has been radiated during 24 hours.

Understanding the state:

According to Mass energy Equivalence

$$E = mc^2 \quad \text{--- (i)}$$

But the given statement mentioned Power, so:

$$P = \frac{E}{t}$$

$$P \cdot t = E \quad \text{--- (ii)}$$

$$10K \cdot 24 \text{ hours}$$

$$10K \cdot 24 \times 60 \times 60 = E$$

$$10K \cdot 43,200 = E$$

$$432,000KJ = E \quad \text{--- (iii)}$$

put the value of (iii) in equation (i) to get "m" so calculating

$$m = 1.44 \text{ kg}$$

$$m = 0.001 \text{ kg}$$

If antenna emit that amount of
Energy.