

Q. The sum of three consecutive prime numbers is 287. Find the square of the middle term.

- DATA:

Sum of three consecutive prime numbers = 287

Three consecutive prime numbers = ?

Square of its middle term = ?

- SOLUTION:

• Find Middle term (or no. close to it).

$$= \frac{\text{Sum of numbers}}{\text{Quantity of numbers}} = \frac{287}{3}$$

$$= \boxed{95.6}$$

This, however, is not a prime no. So,

Choose the nearest prime to '95'.

Prime								Prime
89	90	91	92	93	94	<u>95</u>	96	97

• Hence, nearest prime is, 97 (Middle prime no)

- Justifying the result,

$$89 + 97 + 101 = 287$$

$$\underline{287} = 287 \text{ (LHS = RHS)}$$

• Now,

• Square of Middle term,

$$= (97)^2$$

$$= \boxed{9409}$$

• Three consecutive num. are = 89, 97, 101.

• Square of Middle term = 9409.

Q. The sum of two numbers is 18 and the product of these two numbers is 56. Find the numbers.

- DATA:

Two numbers when added = 18

Two numbers when multiplied = 56

These Numbers = ?

- SOLUTION:

• Let these numbers be = x, y .

• Equating them:

$$x \times y = 56 \rightarrow (1)$$

$$\text{So, } y = \frac{56}{x} \rightarrow (i)$$

$$x + y = 18 \rightarrow (2)$$

• Put (i) in (2)

$$x + y = 18$$

$$x + \frac{56}{x} = 18 \quad (\text{LCM})$$

$$\frac{x^2 + 56}{x} = 18$$

$$x^2 + 56 = 18x$$

$$x^2 - 18x + 56 = 0 \quad (\text{Quadratic Eq.})$$

• Factors Finding.

- Method: 1

2	56	
2	28	$2 \times 2 \times 2 \times 7$
2	14	
2	7	4, 14
	1	

Because of -ve sign in middle : -4, -14

• Method: 2 (Quadratic formula)

$$x^2 - 18x + 56 = 0$$

$\frac{\quad}{a} \quad \frac{\quad}{b} \quad \frac{\quad}{c}$

One method is enough

$$\therefore \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}, \text{ Put values}$$

$$\frac{-18 \pm \sqrt{(18)^2 - 4(1)(56)}}{2(1)}$$

$$\frac{-18 \pm \sqrt{324 - 224}}{2} \Rightarrow \frac{-18 \pm \sqrt{100}}{2}$$

$$\frac{-18 + 10}{2}, \quad \frac{-18 - 10}{2}$$

$$\frac{-8}{2}, \quad \frac{-28}{2}$$

$$-4, \quad -14$$

$$x^2 - 4x - 14x + 56 = 0$$

$$x(x-4) - 14(x-4) = 0$$

$$(x-4)(x-14) = 0$$

$$\text{So, } x = 4 \text{ or } 14$$

Putting value of 'x' in (i)

$$y = \frac{56}{x} \Rightarrow y = \frac{56}{4} \Rightarrow y = 14$$

$$\text{or } x = 14$$

$$y = \frac{56}{14} = y = 4$$

• Concluding,

$$(x = 4, y = 14)$$

OR

$$(y = 14, x = 4)$$

• Justifying,

$$x + y = 18 \Rightarrow 4 + 14 \Rightarrow 18$$

$$x \times y = 56 \Rightarrow 4 \times 14 \Rightarrow 56 \quad (\text{LHS} = \text{RHS})$$

Good attempt!!!