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## IRR Assignment

### CSS 2005

Cash outflow = Rs 40,000

Inflow = Rs 11,652 each year

years (n) = 5

Interest rate = 10%

a) Find NPV

To calculate the NPV, we use the following formula:

$$\text{NPV} = \text{PV of inflows} - \text{PV of Outflows}$$

PV of Outflows = Rs 40,000

PV of inflows for each year is calculated as follows:

n (years)	Cashflow	PV @10%
0	(40,000)	-
1	11,652	$11,652 \div (1.1) = 10592.7$
2	11,652	$11,652 \div (1.1)^2 = 9629.7$
3	11,652	$11,652 \div (1.1)^3 = 8754.3$
4	11,652	$11,652 \div (1.1)^4 = 7958.4$
5	11,652	$11,652 \div (1.1)^5 = 7234.9$
		<u>44170</u>

$$\text{NPV} = 44170 - 40000 \\ = \text{Rs} 4170$$

b) Find IRR

IRR is calculated using the following formula:

$$IRR = r_a + \frac{NPV_a}{NPV_a - NPV_b} (r_b - r_a)$$

where  $r_a$  = lower discount rate chosen

$r_b$  = higher discount rate chosen

$NPV_a$  = NPV at  $r_a$

$NPV_b$  = NPV at  $r_b$

One of the rules to calculate IRR is to have <sup>one</sup> negative NPV. Since the NPV for a project considered by stars Corporation has a positive NPV at  $r = 10\%$ . Let us assume another interest rate at  $20\%$ . NPV and  $r$  have an inverse relationship hence, higher  $r$  might yield a lower NPV.

NPV at  $r = 20\%$  is calculated as:

n	Cashflow	PV @ 20%
0	(40,000)	-
1	11,652	$11,652 / (1.2) = 9710$
2	11,652	$11,652 / (1.2)^2 = 8091.6$
3	11,652	$11,652 / (1.2)^3 = 6743$
4	11,652	$11,652 / (1.2)^4 = 5619.2$
5	11,652	$11,652 / (1.2)^5 = 4682.6$
		<u>34846</u>

$$NPV = 34846 - 40000$$
$$= (5172)$$

~~IRR~~ For IRR, let

$$r_a = 10\%$$

$$NPV_a = 4170$$

$$r_b = 20\%$$

$$NPV_b = -5172$$

Computing these values into IRR equation:

$$\begin{aligned} IRR &= r_a + \frac{NPV_a}{NPV_a - NPV_b} (r_b - r_a) \\ &= 0.1 + \frac{4170}{4170 - (-5172)} (0.2 - 0.1) \end{aligned}$$

$$IRR = 14.4\%$$

CSS 2013 . Q9 :

Cash outflow = \$800,000

$n = 4$  years , tax bracket = 50%

Cash inflow:  $y_1 = \$200,000$ ,  $y_2 = \$250,000$

$y_3 = \$300,000$  and  $y_4 = \$400,000$

a) If required rate of return = 15% , what is NPV and is it acceptable?

To calculate the NPV, we first use the following formula:

$$NPV = PV \text{ of inflows} - PV \text{ of outflows}$$

PV of inflows with rate 15% for 4 years is calculated as follows:

n	Cashflow	PV @ 15%
0	(800,000)	-
1	200,000	$200,000 / (1.15) = 173913$
2	250,000	$250,000 / (1.15)^2 = 189035.9$
3	300,000	$300,000 / (1.15)^3 = 197254.8$
4	400,000	$400,000 / (1.15)^4 = 228701.2$
		<u>788905</u>

$$\text{NPV} = 788905 - 800000$$

$$= -11094$$

Since the NPV is negative, this project is not acceptable. This means that the expected cashflows from the project will not provide a return greater than the required rate of return of 15%.

b) Find its Internal Rate of Return (IRR)

IRR is calculated using the following formula:

$$\text{IRR} = r_a + \frac{\text{NPV}_a}{\text{NPV}_a - \text{NPV}_b} (r_b - r_a)$$

Since NPV was negative at  $r=15\%$ . Let's assume a lower NPV at 5%. As NPV and rate of interest ( $r$ ) have an inverse relationship, a lower ~~NPV~~  $r$  may yield a positive NPV.

Calculation for NPV at  $r=5\%$  is

as follows:

n	CashFlow	PV@5%
0	(800,000)	-
1	200,000	$200,000 \div (1.05) = 190476.1$
2	250,000	$250,000 \div (1.05)^2 = 226757.3$
3	300,000	$300,000 \div (1.05)^3 = 259151.2$
4	400,000	$400,000 \div (1.05)^4 = 329080.9$
		<u>1005465</u>

$$\text{NPV} = 1005465 - 800000$$
$$= 205465$$

For IRR, let

$$r_a = 5\%$$

$$\text{NPV}_a = 205465$$

$$r_b = 15\%$$

$$\text{NPV}_b = -11094$$

$$\text{IRR} = r_a + \frac{\text{NPV}_a}{\text{NPV}_a - \text{NPV}_b} (r_b - r_a)$$
$$= 0.05 + \frac{205465}{205465 - (-11094)} (0.15 - 0.05)$$
$$= 0.594$$

$$\text{IRR} = 59.4\%$$

(P.T.O)

## CSS 2018 (A&A)

ABC Company considers a new project:

Cash outflows:  $y_0 = 700,000$  &  $y_1 = 1,000,000$

Cash inflows:  $y_2 = 250,000$ ,  $y_3 = 300,000$ ,

$y_4$  to  $y_{10} = 400,000$  (annually)

a) Calculate NPV when  $r = 15\%$ . Is it acceptable?

To calculate NPV, we use the following formula:

$$\text{NPV} = \text{PV of inflows} - \text{PV of outflows.}$$

PV of inflows and outflow at rate 15% from  $y_0$  to  $y_3$  is as follows:

n	Cashflow	PV@15%
0	(700,000)	-
1	(1,000,000)	$1,000,000 \div (1.15) = 869565.2$
2	250,000	$250,000 \div (1.15)^2 = 189035.9$
3	300,000	$300,000 \div (1.15)^3 = 197254.8$

Since  $y_4$  to  $y_{10}$  has a constant cashflow received annually at the rate of 15%, it can be calculated using Present Value Annuity Ordinary formula:

$$\text{PV of Annuity} = P \left[ \frac{1 - (1+i)^{-n}}{i} \right]$$

where  $P$  = cash inflow,  $i$  = interest rate and  $n$  = number of years

Computing values of ABC company into the equation above:

$$PV = 400,000 \left[ \frac{1 - (1 + 0.15)^{-6}}{0.15} \right]$$

$$= 1513793$$

$$PV \text{ inflows} = 189035.9 + 197254.8 +$$

$$1513793$$

$$= 1900083$$

$$PV \text{ outflows} = 700,000 + 869565.2$$

$$= 1569565$$

$$NPV = 1900083 - 1569565$$

$$= 330,518$$

Since the NPV is positive, this project is acceptable. The present value of benefits exceeds the present value of costs at the rate of return at 15%.

b) Find its Internal Rate of Return (IRR)

IRR is calculated using the following formula:

$$IRR = r_a + \frac{NPV_a}{NPV_a - NPV_b} (r_b - r_a)$$

Since NPV was positive at  $r = 15\%$ . Let us assume a higher NPV at 25%. As NPV and interest rate ( $r$ ) have an <sup>inverse</sup> ~~inverse~~ relationship, a higher  $r$  may yield a lower NPV. Calculations for NPV at 25% are as follows:

PV of inflows and outflows at  $r=25\%$ .  
 From  $y_0$  to  $y_3$ :

n	Cashflow	PV@ 25%
0	(700,000)	-
1	(1,000,000)	$1,000,000 \div (1.25) = 800,000$
2	250,000	$250,000 \div (1.25)^2 = 160,000$
3	300,000	$300,000 \div (1.25)^3 = 153,600$

Since  $y_0$  to  $y_3$  has a constant cashflow at  $r=25\%$ . PV can be calculate using

$$PV \text{ Annuity Ordinary} = P \left[ \frac{1 - (1+i)^{-n}}{i} \right]$$

$$= 400,000 \left[ \frac{1 - (1+0.25)^{-6}}{0.25} \right]$$

$$= 1,180,569.6$$

$$PV \text{ inflows} = 160,000 + 153,600 + 1,180,569.6$$

$$= 1,494,169.$$

$$PV \text{ outflows} = 700,000 + 800,000$$

$$= 1,500,000$$

$$NPV = PV \text{ of inflows} - PV \text{ of outflows}$$

$$= 1,494,169 - 1,500,000$$

$$= -5831$$

For IRR let  $r_a = 15\%$ ,  $r_b = 25\%$ ,  
 $NPV_a = 330,518$ ,  $NPV_b = -5831$

$$IRR = 0.15 + \frac{330518}{330518 - (-5831)} (0.25 - 0.15)$$

$$= 24.8\%$$



### Example #1.

Cash outflow: Rs 213,000,  $n = 4$  years

Cash inflow:  $y_1 = 65,200$ ,  $y_2 = 96,000$ ,  $y_3 = 73,100$

$y_4 = 55,400$

Find IRR.

### Solution:

To calculate IRR, the following formula is used:

$$IRR = r_a + \frac{NPV_a}{NPV_a - NPV_b} (r_b - r_a)$$

where  $r_a$  = lower discount rate,

$r_b$  = higher discount rate,

$NPV_a$  = NPV at  $r_a$ , and

$NPV_b$  = NPV at  $r_b$ .

For <sup>lower</sup> ~~lower~~ discount rate, let  $r_a = 10\%$ .

NPV<sub>a</sub> will be calculated as:

n	Cash-flow	PV @ 10%
0	(213,000)	—
1	65,200	$65,200 \div (1.1) = 59,272.7$
2	96,000	$96,000 \div (1.1)^2 = 79,338.8$
3	73,100	$73,100 \div (1.1)^3 = 54,921.1$
4	55,400	<del>55,400</del> $55,400 \div (1.1)^4 = 37,838.9$
		Rs. 231,371

$$NPV_a = \text{PV of Inflow} - \text{PV of Outflow}$$
$$= 231,371 - 213,000$$

$$NPV_a = \text{Rs. } 18,371$$

For higher discount rate, let  $r = 20\%$ .  
 NPV calculation is as follows:

n	Cashflow	PV@20%
0	(213000)	-
1	65,200	$65200 \div (1.2) = 54333.3$
2	96,000	$96000 \div (1.2)^2 = 66666.6$
3	73,100	$73100 \div (1.2)^3 = 42303.2$
4	55,400	$55400 \div (1.2)^4 = 26716.8$
		Rs. 190020

$$NPV_2 = 190020 - 213000$$

$$= \text{Rs.} - 22980$$

$$IRR = r_a + \frac{NPV_a}{NPV_a - NPV_b} (r_b - r_a)$$

$$= 0.1 + \frac{18371}{18371 - (-22980)} (0.20 - 0.10)$$

$$= 0.144$$

$$= 14.4\%$$

## Example # 2.

Cash outflow: Rs 500,000,  $n = 4$  years

Cash inflow: Rs. 160,000 each year

Sale of equipment at  $n = 4$ : Rs 50,000

Interest rate = 10%. Calculate IRR.

**Solution:**

IRR is calculated using the following formula

$$IRR = r_a + \frac{NPV_a}{NPV_a - NPV_b} (r_b - r_a)$$

where  $r_a$  = lower discount rate,

$r_b$  = higher discount rate,

$NPV_a$  = NPV at  $r_a$ , and

$NPV_b$  = NPV at  $r_b$

For lower discount rate, let  $r_a = 10\%$ .

NPV will be calculated as:

n	Cashflow	PV@10%
0	(500,000)	—
1	160,000	$160,000 / (1.1) = 145454.5$
2	160,000	$160,000 / (1.1)^2 = 132231.4$
3	160,000	$160,000 / (1.1)^3 = 120210.3$
4	160,000 + 50,000	$210,000 / (1.1)^4 = 143432.8$
		Rs. 541329

$$\begin{aligned} NPV &= PV \text{ inflows} - PV \text{ outflows} \\ &= 541329 - 500000 \\ &= \text{Rs. } 41329 \end{aligned}$$

For higher discount rate, let  $r_b = 20\%$

$NPV_b$  is calculated as follows:

n	Cashflows	PV @ 20%
0	(500,000)	—
1	160,000	$160,000 \div (1.2) = 133333.3$
2	160,000	$160,000 \div (1.2)^2 = 111111.1$
3	160,000	$160,000 \div (1.2)^3 = 92592.5$
4	210,000	<del><math>110,000 \div (1.2)^4</math></del> $210,000 \div (1.2)^4 = 101273.1$
		<hr/> Rs. 438310

$$NPV_b = 438,310 - 500,000$$
$$= \text{Rs. } -61690$$

$$IRR = r_a + \frac{NPV_a}{NPV_a - NPV_b} (r_b - r_a)$$
$$= 0.1 + \frac{41329}{41329 - (-61690)} (0.20 - 0.10)$$
$$= 0.14$$

$$IRR = 14\%$$